



# **A BI-OBJECTIVE MODEL FOR HANDICAPPED TRANSPORTATION**

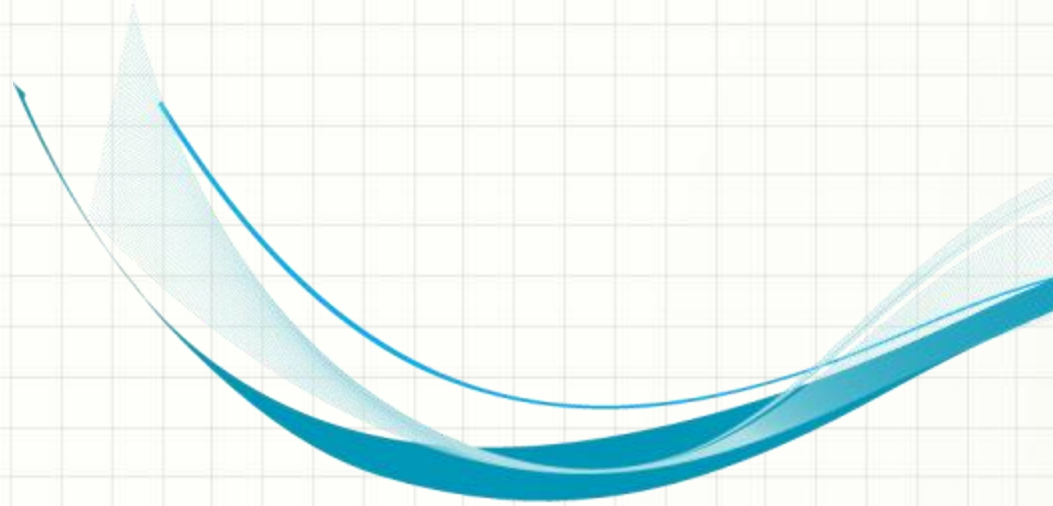
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# Introduction

- A Bi-objective model
- Description of objectives function
- References about (Dial A Ride Problem) DARP
- Solutions Approach



- Transportation of a set of handicapped people (clients), from the corresponding homes to the destinations (cultural centers, hospitals, etc.)
- Design of routes following the DARP. This model incorporates the “human perspective” (Cordeau, 2003)



Cordeau 2003: Tabu


Cordeau 2006: Formulation

Cordeau and Laporte (2007): revision of models and approaches

Mauri and Lorena (2006): A multi-objective model

Paquette et al. (2012), (2013): Real problem in Canada, involves quality of service, and use of Tabu

Chevrier et al. (2012): A three objectives model



Guerriero et al (2014): 2 objectives, total time and waiting time

Muelas et al (2015): Large size problems with VNS

Ritzinger et al (2016): Large Neighborhood Search

Chassaing et al (2016): Evolutive Local Search

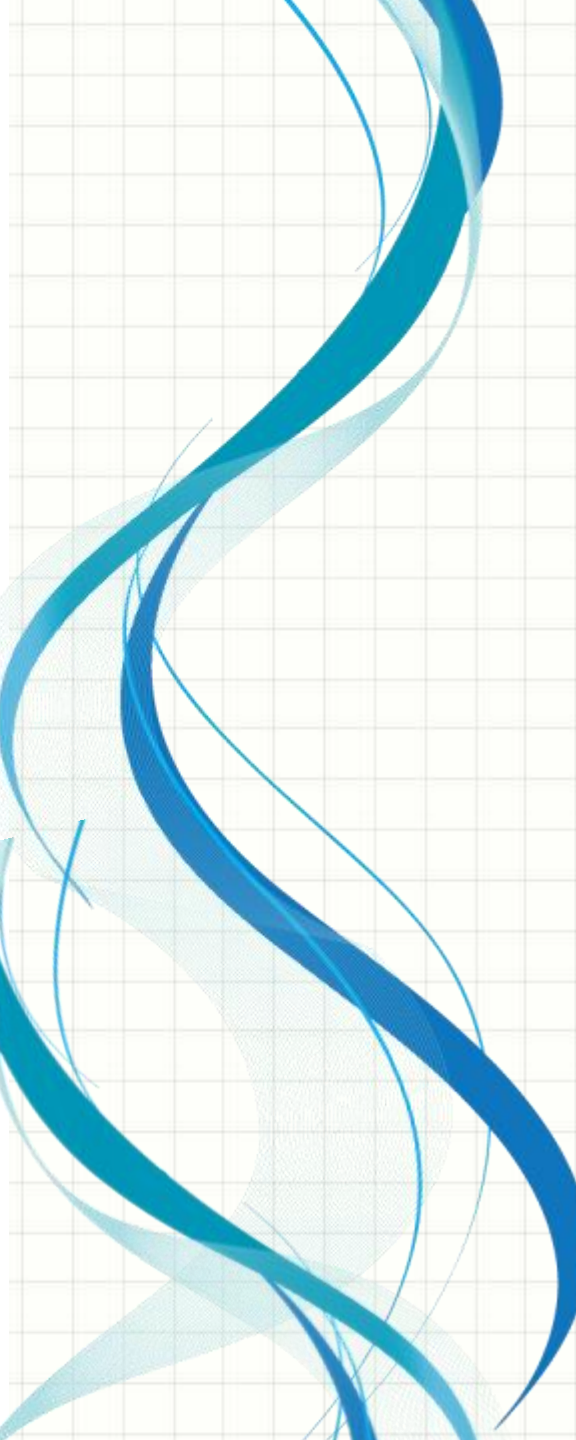
Molenbruch et al (2017): Total time and total distance



A decorative graphic on the left side of the slide, consisting of a thick blue wavy line that curves upwards and then downwards. It is surrounded by lighter blue, semi-transparent wavy lines and small arrows pointing in the direction of the flow.

## Two objectives:

- Minimization Transport Costs
- Maximize the level service (minimizing “over” time)



Set of clients  $W = \{w_1, w_2, w_3, \dots, w_n\}$

Initial points  $P = \{1, 2, 3, \dots, n\}$

Destinations  $D = \{n+1, n+2, \dots, 2 \cdot n\}$

$$V = P \cup D \cup \{0\}$$

$L_{max}$  : Maximum travel time by vehicle

$m$  : number of vehicles

$Q$  : Capacity,       $C$  : Vehicle Cost

$t_{ij}, d_{ij}$  : time and distances matrices



Economic objective

Used Vehicles·C + Total distance

Social objective

$$\min \max \{ |T_i - t_{i_{n+i}}| : i \in \{1, 2, \dots, n\} \}$$

$T_i$  : Time of travel of client  $w_i$  in a solution  $S$

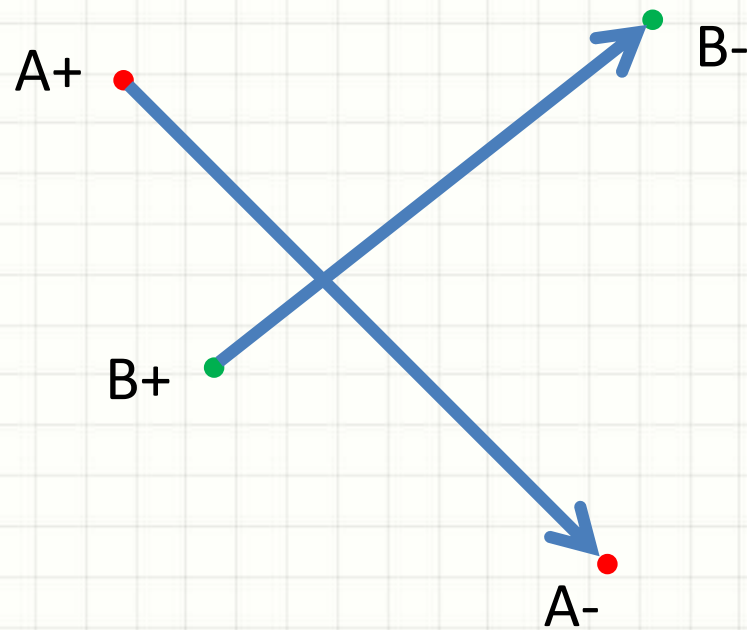


$A^+$  ●

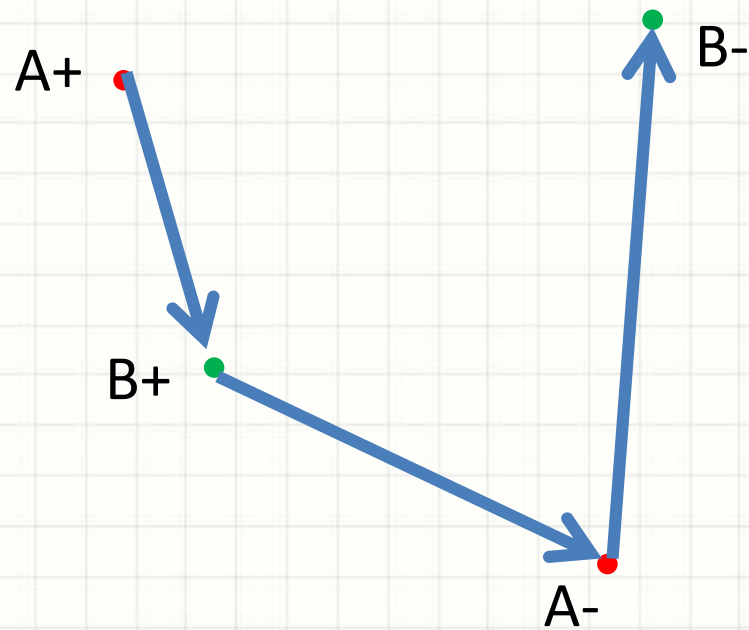
●  $B^-$

$B^+$  ●

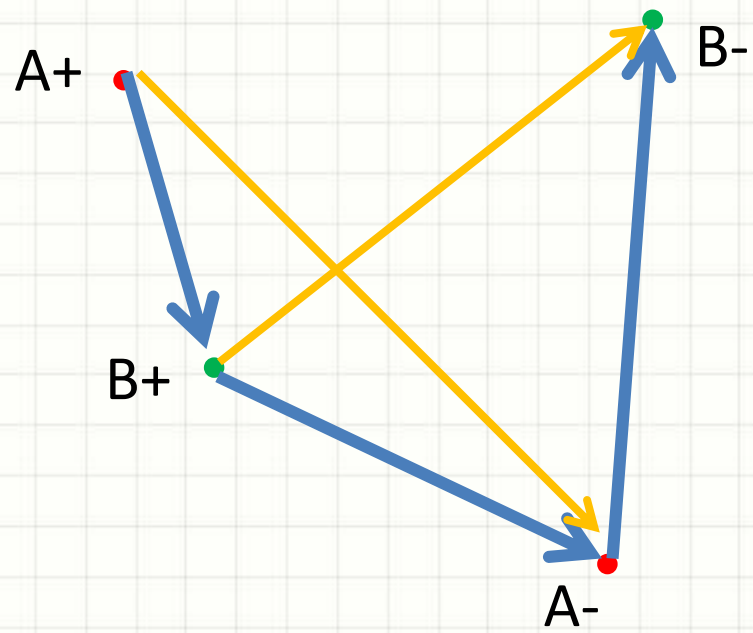
$A^-$  ●

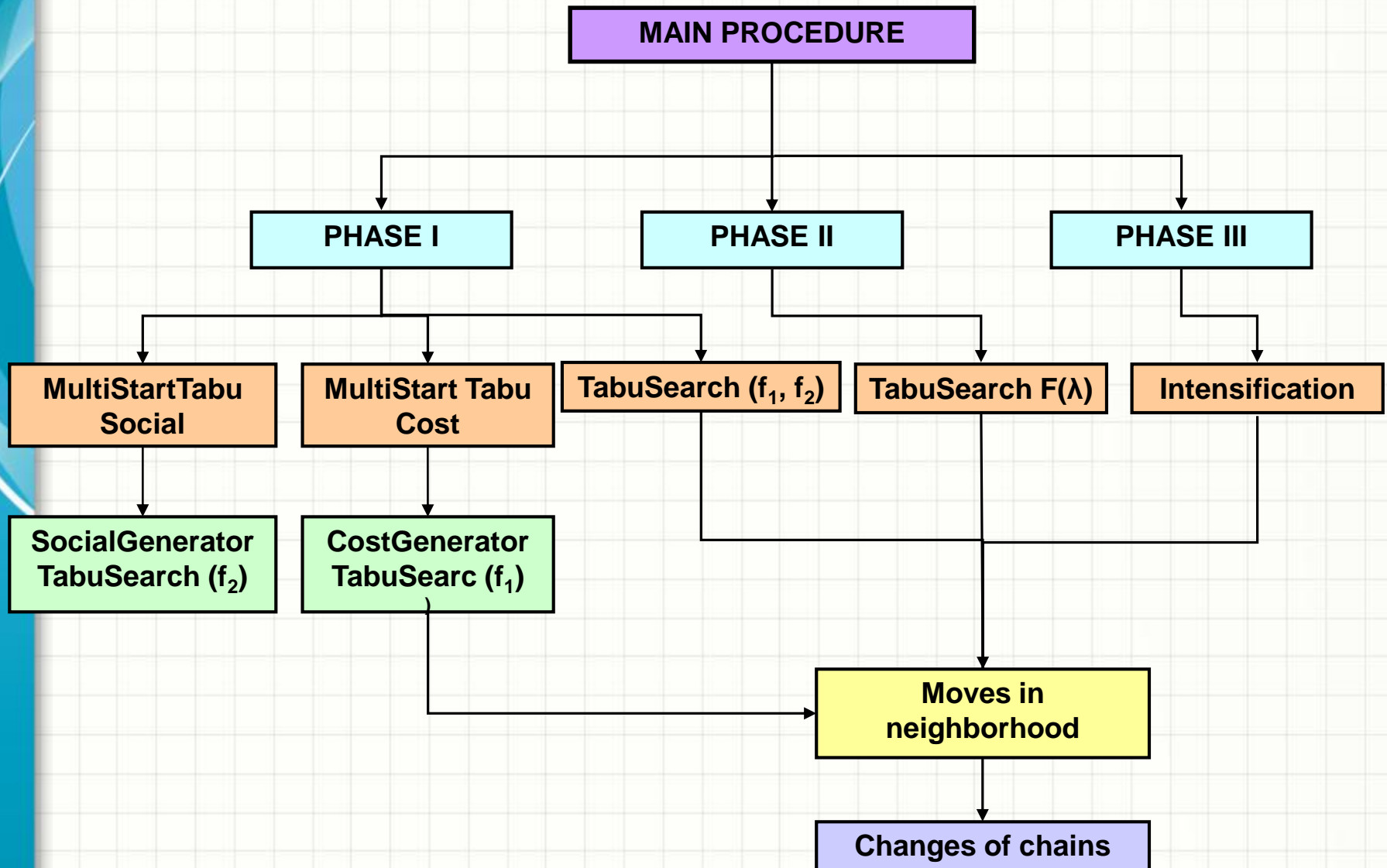


Social solution:  $T_A = t_{A^+ A^-}$  and  $T_B = t_{B^+ B^-}$



Economic solution: 1 vehicle







- $S$  : Feasible solution
- $f_1(S)$  = Cost in  $S$
- $f_2(S)$  = Social function in  $S$
- $f_1^{\min}$  y  $f_1^{\max}$  : Min and max values for  $f_1$  in Set of No-dominated solutions
- $f_2^{\min}$  y  $f_2^{\max}$  : the same for  $f_2$

$$F_{\lambda}(S) = \max \left\{ \lambda \cdot \frac{f_1(S) - f_1^{\min}}{f_1^{\max} - f_1^{\min}}, (1 - \lambda) \cdot \frac{f_2(S) - f_2^{\min}}{f_2^{\max} - f_2^{\min}} \right\}$$

Calculate  $d_{0i+} + d_{i+i-} + d_{i-0}$

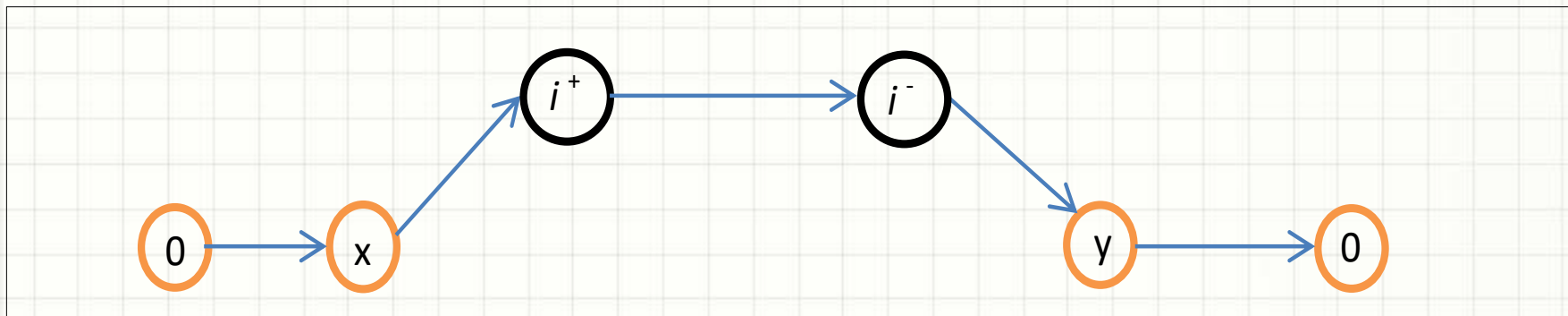
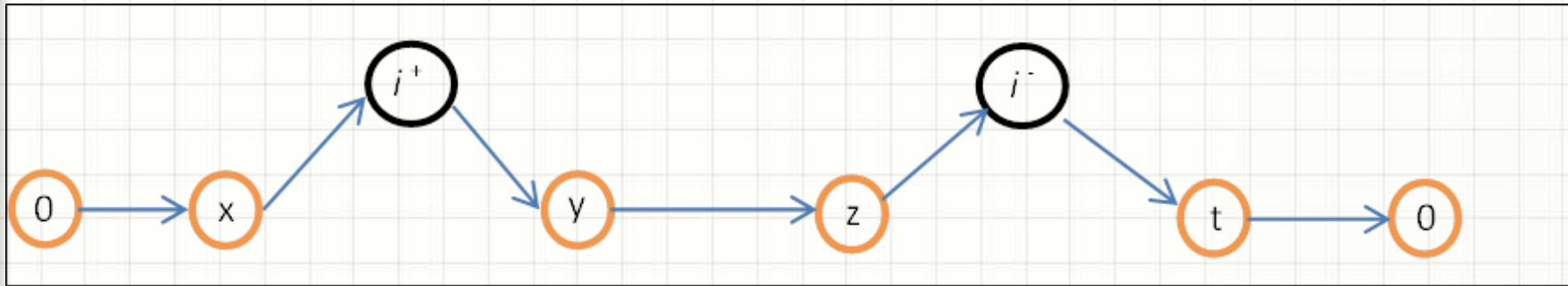
In every iteration take the next client  $i$

Built the set  $L$  of all feasiabes insertions of  $i$

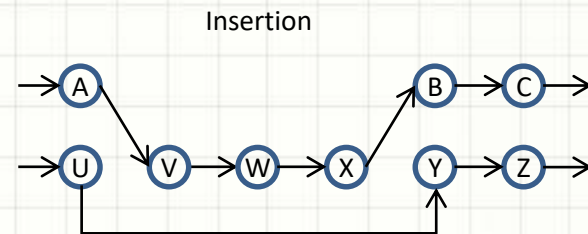
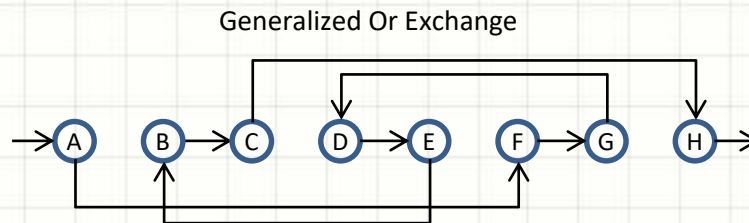
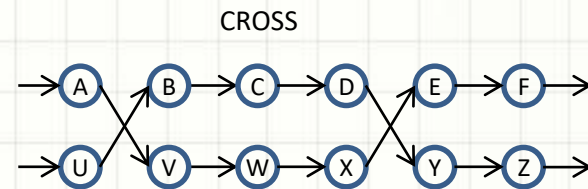
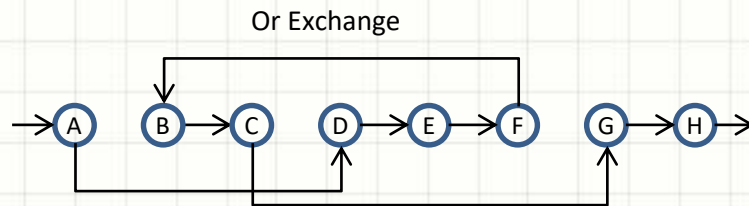
Calculate  $\Delta d(ins)$  and  $\Delta f(ins) : ins \in L$

$$val(ins) = \beta \left( \frac{\Delta d(ins) - \min \Delta d}{\max \Delta d - \min \Delta d} \right) + (1 - \beta) \left( \frac{\Delta f(ins) - \min \Delta f}{\max \Delta f - \min \Delta f} \right)$$

Built *ListCandidate* with the  $ins$  corresponding with the minimun  $val(ins)$  values



# TABU SEARCH : MOVES



Check the feasibility:

Total time

Capacity

Preferences: A+ before A-

Auxiliar Variables that are updated afer each move

*TimeAc(i)* : Accumulated distance after visiting i

*Qac(i)* : Accumulated passangers after visiting i

List of chains that can be moved in Inter-routes

List of moves that can be performed (Intra Routes)

*max\_desp*("chain") :

maximum numer os positions that  
chain can be moved ahead (forward)



**QUESTIONS?**

