







Greener Fleet Configurations for the Heterogeneous Vehicle Routing Problem with Multiple Capacities and Driving Ranges

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Outline

- ✓ Vehicle Routing Problem with Multiple Driving ranges (VRPMD)
- ✓ Capacitated Vehicle Routing Problem with Multiple Driving ranges (CVRPMD)
- ✓ Proposed solution method
- ✓ Analysis of the results
- ✓ Conclusion and future work



Vehicle Routing Problem with Multiple Driving ranges (VRPMD)





Contents lists available at ScienceDirect

Applied Soft Computing

journal homepage: www.elsevier.com/locate/asoc

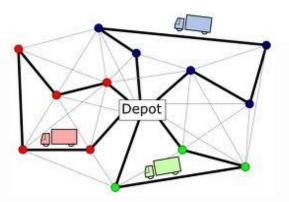


Routing fleets with multiple driving ranges: Is it possible to use greener fleet configurations?



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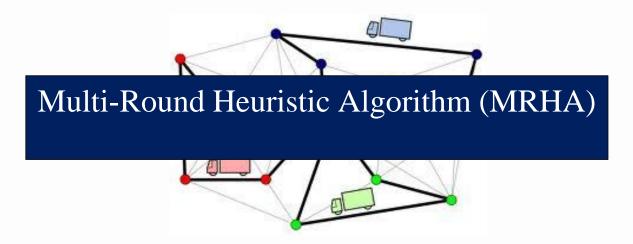
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Vehicle Routing Problem with Multiple Driving ranges (VRPMD)

| | Vehicle Type | Vehicle capacity | Vehicle driving ranges (distance unit) | Symbol |
|---|--|------------------|--|--------|
| | ICEVs ¹ and/or PHEVs ² | Fixed to | No driving range limitation –Large | L |
| 9 | EVs | 100 | 200 – Medium | M |
| | EVs | | 100 - Small | S |



¹Internal Combustion Engine Vehicles

²Plug-in Hybrid Electric Vehicles



Capacitated Vehicle Routing Problem with Multiple Driving ranges (CVRPMD)

| Vehicle Type | Vehicle capacity | Vehicle driving ranges (distance unit) | Symbol |
|--|--------------------|--|--------|
| ICEVs ¹ and/or PHEVs ² | 1.25Q ₀ | No driving range limitation –Large | L |
| EVs | Q_0 | 200 – Medium | M |
| EVs | $0.8Q_{0}$ | 100 – Small | S |

Develop an efficient solution method:

Multi-Round Iterated Greedy

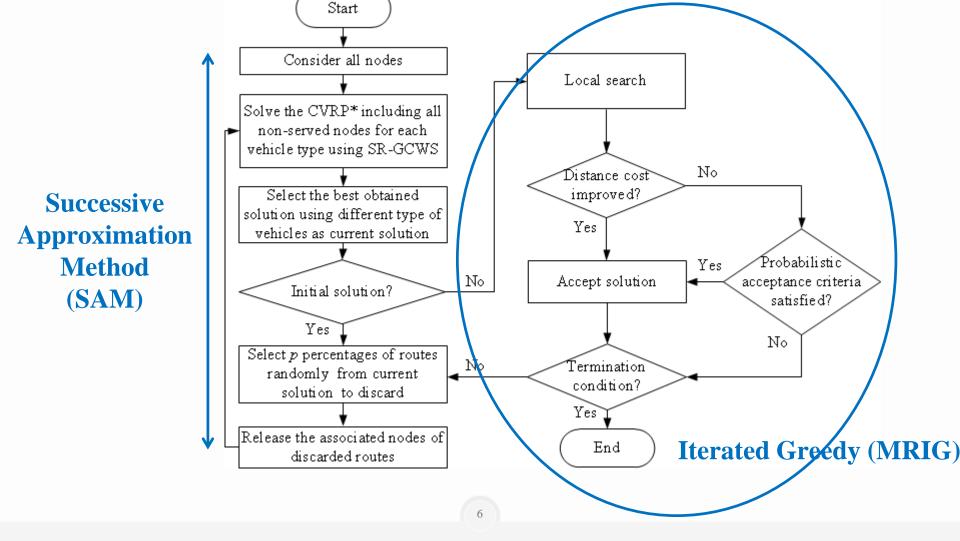
¹Internal Combustion Engine Vehicles

²Plug-in Hybrid Electric Vehicles



Proposed solving method

Multi-Round Iterated Greedy (MRIG)





Analysis of the results

- ✓ 33 CVRP classical benchmark instances to solve both VRPMD and CVRPMD- are selected from a large number of instances
- ✓ using different criteria to select these benchmark instances
 - instances with an optimal or pseudo-optimal solution (instances from sets A, B, E, F, M and P)
 - instances with information on routes for the optimal or pseudo-optimal solution
 - mid-size instances including between 22 and 135 nodes.



Distance-based cost evaluation

Measure the performance of the results by Relative Percentage Difference (RPD)

$$RPD = \frac{Alg_{sol} - Best_{sol}}{Best_{sol}} \times 100$$

 $Best_{sol}$: the best distance-based cost found through our results and the existing ones by Juan et al. (2014b), and the best known solutions (BKS) for any instance.

 Alg_{sol} : the distance-based cost obtained by the proposed algorithm



Novel green indices for fleet configurations

$$GI_1 = \frac{S + \omega M}{S + M + L}$$

 $\omega \in [0, 1]$.

The number of the used vehicle of types S, M and L are denoted by S,

M and L, respectively.

The values of ω is set to 0.7.



Novel green indices for fleet configurations

$$GI_2 = \gamma S + \beta M + \alpha L$$

This index measures environmental unit cost for each fleet configuration.

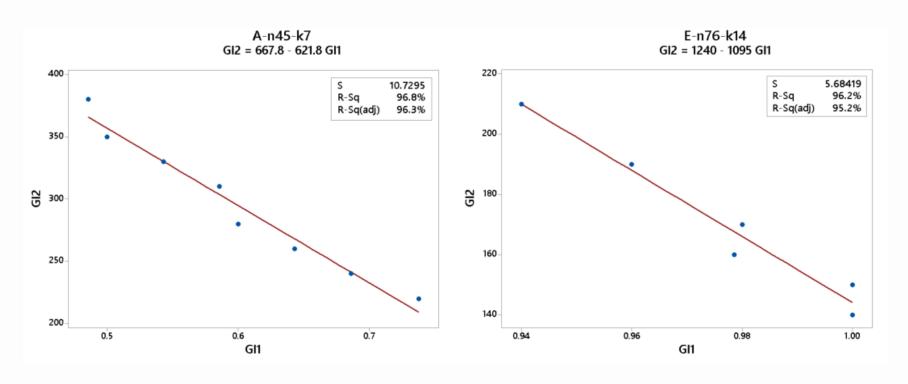
The values of $\alpha = 100$

$$\beta = 30$$

and
$$\gamma = 10$$
.



Relation between Novel green indices





| Instance name | Number of | a | BKS | MRHA | | MR | IG | RPD | | Diversified |
|------------------|-----------|----------|--------------|-----------------------|---------|-----------------------|---------|-------|-------|-------------|
| | nodes | Capacity | | Fleet CFG . $S/M/L$ | DBCost | Fleet CFG . $S/M/L$ | DBCost | MRHA | MRIG | Ratio |
| | | | | 2/5/3 | 1776.19 | 2/5/3 | 1775.75 | 0.55 | 0.52 | |
| | | | | 1/7/2 | 1785.05 | 1/7/2 | 1785.04 | 1.05 | 1.05 | |
| A-n80-k10 | 80 | 100 | 1766.50 | | | 2/6/2 | 1794.42 | - | - | 2.5 |
| | | | | | | 0/9/1 | 1994.16 | - | - | |
| | | | | | | 2/8/1 | 2016.21 | - | - | |
| | | | | 0/4/5 | 1602.29 | 0/4/5 | 1602.29 | 0.00 | 0.00 | |
| | | | | 0/5/4 | 1603.37 | 0/5/4 | 1603.37 | 0.07 | 0.07 | |
| | | | | 0/6/3 | 1631.66 | 0/6/3 | 1631.85 | 1.83 | 1.84 | |
| B-n57-k9 | 57 | 100 | 1603.63 | 1/3/5 | 1642.53 | 1/3/5 | 1636.34 | 2.51 | 2.13 | 1.6 |
| 2 1101 110 | ٥. | 100 | 1000.00 | 1/4/4 | 1646.65 | 1/4/4 | 1637.44 | 2.77 | 2.19 | 1.0 |
| | | | | | | 1/5/3 | 1650.87 | - | - | |
| | | | | | | 2/2/6 | 1694.09 | - | - | |
| | | | | | | 0/7/2 | 1707.81 | - | - | |
| | | 4500 | 535.80 | 1/3/0 | 505.01 | 1/3/0 | 505.01 | 0.00 | 0.00 | |
| E-n30-k3 | 20 | | | | | 2/1/1 | 579.78 | - | - | 4 |
| E-n30-k3 | 30 | 4500 | 555.80 | | | 3/0/2 | 597.65 | - | - | 4 |
| | | | | | | 3/1/1 | 633.37 | - | - | |
| | | | | 3/1/3 | 1175.73 | 3/1/3 | 1168.01 | 0.66 | 0.00 | |
| | | | | 3/2/2 | 1190.07 | 3/2/2 | 1175.68 | 1.89 | 0.66 | |
| F-n135-k7 | 135 | 2210 | 1170.65 | , , | | 2/3/2 | 1171.18 | - | - | 2.5 |
| | | | | | | 1/5/1 | 1215.14 | - | - | |
| | | | | | | 2/4/1 | 1241.70 | - | - | |
| | | 2/3/ | 2/3/2 | 1047.96 | 2/3/2 | 1044.64 | 0.32 | 0.00 | | |
| M - 101 l-7 | 101 | 200 | 1045 10 | 1/7/0 | 1274.60 | 1/7/0 | 1287.52 | 22.01 | 23.25 | 0 |
| M-n121-k7 | 121 | 200 | 1045.16 | , , | | 3/2/3 | 1050.66 | - | - | 2 |
| | | | | | | 1/5/1 | 1129.40 | - | - | |
| | | | | 8/2/0 | 834.38 | 8/2/0 | 843.63 | 0.53 | 1.64 | |
| | | | | 10/0/0 | 841.56 | 10/0/0 | 851.39 | 1.39 | 2.57 | |
| P-n70-k10 | 70 | 135 | 830.02 | /-/- | | 6/4/0 | 841.42 | - | 1.37 | 2.5 |
| 1-H70-K10 | | | - | | | 9/1/0 | 844.35 | - | - | |
| | | | | | | 7/3/0 | 842.36 | _ | - | |

Experimental results for 20 classical CVRP instances

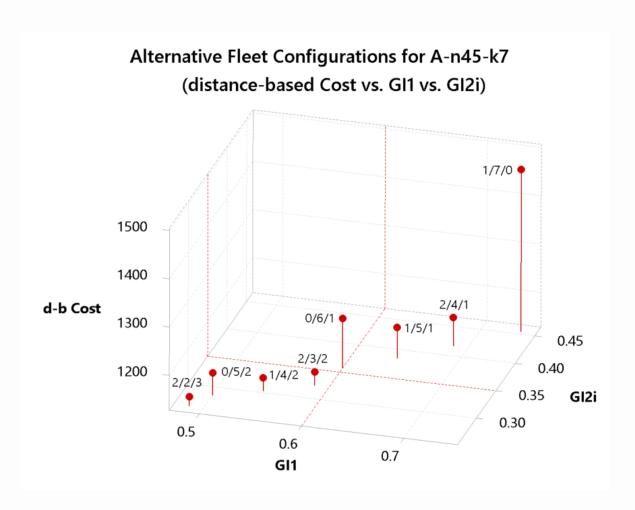


| Instance name | Number of nodes | Capacity | BKS | MRIG | RPD | | |
|---------------|-----------------|--|---|-----------------------|--------------|-------|--|
| | | | | Fleet CFG . $S/M/L$ | Cost | | |
| | | | | 2/2/3 | 1146.77 | 0.00 | |
| | | | | 1/4/2 | 1154.43 | 0.67 | |
| | | | | 2/3/2 | 1155.60 | 0.77 | |
| A-n45-k7 | 45 | · · · | 1191.29 | 3.88 | | | |
| | | | | 0/5/2 | 1174.01 | 2.38 | |
| | | | | 0/6/1 | 1230.27 | 7.28 | |
| | | | | 1/7/0 | 1463.93 | 27.66 | |
| | | | | 2/4/1 | 1186.46 | 3.46 | |
| | | | | 3/4/0 | 690.20 | 0.38 | |
| F 70 17 | 70 | $\frac{76}{220}$ 687.60 $\frac{4}{3}$ /0 | 00 7 00 | | 695.26 | 1.11 | |
| E-n76-k7 | 76 | | | 705.97 | 2.67 | | |
| | | | | 6/1/0 | 733.74 | 6.71 | |
| D 45 1 4 | 4 ~ | 2010 | 704 57 | 1/2/1 | 723.54 | 0.00 | |
| F-n45-k4 | 45 | 2010 | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ | 792.37 | 9.51 | | |
| | | | | 0/3/1 | 0/3/1 691.29 | 0.00 | |
| | | | | 0/4/0 | 694.67 | 0.49 | |
| P-n101-k4 | 101 | 400 | 692.28 | 1/1/2 | 703.91 | 1.83 | |
| | | | | 1/2/1 | 700.88 | 1.39 | |
| | | | | 2/3/0 | 729.90 | 5.59 | |

Experimental results for additional classical VRP instances

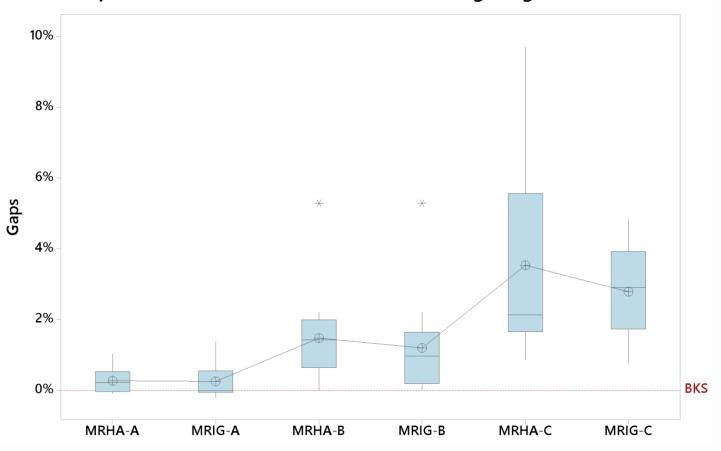


$$GI_2i = 1/GI_2$$





Gaps w.r.t. the BKS of the VRP without driving-range limitations





| | | | $SetGI_1$ | | | | | $SetGI_2$ | | | | | |
|---|-------------------------|-------------|---|---|------------------------------|-------------------------|--------------------------------|---|-----------------------------|----------------------|--------------------|------------------------|--|
| $\begin{array}{c} {\rm Instance} \\ {\rm name} \ (Q_0) \end{array}$ | $_{\rm Cost}^{\rm BKS}$ | VS-VM-VL | Fleet CFG. S/M/L | DBCost | GI_1 | GI_2 | RPD | Fleet CFG. S/M/L | DBCost | GI_1 | GI_2 | RPD | |
| P-n40-k5(140) | 461.73 | 112-140-175 | $0/1/3$ $0/0/4^{L_S}$ $3/0/3^{L_m}$ $6/0/0^{L_l}$ | 431.67 432.23 457.78 514.97 | 0.18 0.00 0.50 1.00 | 330 400 330 60 | 0.00 0.13 6.05 19.30 | $2/0/4^{L}s$ $4/0/2^{L}m$ $6/0/0^{L}l$ | 584.80 463.83 514.97 | 0.33 0.67 1.00 | 420 240 60 | 35.47 7.45 19.30 | |
| P-n50-k10(100) | 699.56 | 80-100-125 | $0/0/8^{L_S} \ 5/0/5^{L_m} \ 13/0/0^{L_l}$ | 607.39 669.00 805.71 | $0.00 \\ 0.50 \\ 1.00$ | 800 550 130 | 0.00 10.14 32.65 | $0/1/8^{L_S} \ 0/6/3^{L_m} \ 13/0/0^{L_l}$ | 658.36 657.15 805.71 | 0.08 0.47 1.00 | 830 480 130 | 8.39 8.19 32.65 | |
| P-n55-k15(70) | 991.48 | 56-70-87 | $0/0/13^{L_S} \ 8/0/8^{L_m} \ 20/0/0^{L_l}$ | 824.21 915.58 1126.70 | $0.00 \\ 0.50 \\ 1.00$ | 1300 880 200 | 0.00 11.09 36.70 | $0/1/13^{L_S} \ 3/8/4^{L_m} \ 20/0/0^{L_l}$ | 883.51 919.94 1126.70 | 0.05 0.57 1.00 | 1330 670 200 | 7.20 11.62 36.70 | |
| P-n65-k10(130) | 796.67 | 104-130-162 | $0/0/8^{L_S} \ 5/0/5^{L_m} \ 13/0/0^{L_l}$ | 726.51 779.95 931.96 | $0.00 \\ 0.50 \\ 1.00$ | 800 550 130 | 0.00 7.36 28.28 | $\frac{3/0/8^L s}{0/6/3^L m}$ $\frac{13/0/0^L l}{13}$ | 831.83 766.30 931.96 | 0.27 0.47 1.00 | 830 480 130 | 14.50 5.48 28.28 | |
| P-n70-k10(135) | 830.02 | 108-135-196 | $0/0/8^{L_S} \ 5/0/5^{L_m} \ 13/0/0^{L_l}$ | 760.93 821.68 969.13 | 0.00 0.50 1.00 | 800 550 130 | 0.00 7.98 27.36 | $\frac{1/1/8^L s}{1/6/3^L m}$ $\frac{13/0}{0^L l}$ | 916.60 812.82 969.13 | 0.17 0.52 1.00 | 840 490 130 | 20.46 6.82 27.36 | |
| P-n76-k4(350) | 598.22 | 280-350-437 | $1/1/2$ $0/0/4^Ls$ $2/0/2^Lm$ $8/0/0^Ll$ | 594.64 695.78 606.86 744.71 | 0.43 0.00 0.50 1.00 | 240 400 220 80 | 0.00 17.01 2.06 25.24 | $2/1/4^{L_S} \ 0/2/2^{L_m} \ 8/0/0^{L_l}$ | 935.17 597.13 744.71 | 0.39 0.35 1.00 | 450 260 80 | 57.27 0.42 25.24 | |

Experimental results for CVRPMD with classical VRP instances



Conclusion and future work

- ☐ Extending the VRPMD:
 - Multiple capacities for each type of vehicles
 - developing an efficient method (MRIG)
- ☐ Developing reasonable solutions in terms of distance-based cost and more diverse solutions in terms of using greener fleet configurations.
- ☐ Help decision makers to decide the best routes for their managerial problems



Conclusion and future work

- ☐ Multi-objective optimization models
- ☐ integrating classical assumptions such as time windows and multi-depot
- ☐ Considering the impact of the carrying load of the vehicles on the resource consumption

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