# Greener Fleet Configurations for the Heterogeneous Vehicle Routing Problem with Multiple Capacities and Driving Ranges 

Sara Hatami, Majid Eskandarpour, Manuel Chica, Djamila Ouelhadj, Angel A. Juan

Department of Computer Science, IN3 - Open University of Catalonia, 08018 Barcelona, Spain


## Outline

$\checkmark$ Vehicle Routing Problem with Multiple Driving ranges (VRPMD)
$\checkmark$ Capacitated Vehicle Routing Problem with Multiple Driving ranges (CVRPMD)
$\checkmark$ Proposed solution method
$\checkmark$ Analysis of the results
$\checkmark$ Conclusion and future work

# Vehicle Routing Problem with Multiple Driving ranges (VRPMD) 

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Routing fleets with multiple driving ranges: Is it possible to use greener fleet configurations?

Angel A. Juan ${ }^{\text {a,* }, ~ J a r r o d ~ G o e n t z e l ~}{ }^{\text {b }}$, Tolga Bektaş ${ }^{\text {c }}$
a IN3 - Open University of Catalonia, Barcelona, Spain
${ }^{\mathrm{b}}$ Massachusetts Institute of Technology, Cambridge, USA
University of Southampton, Southampton, UK


## Vehicle Routing Problem with Multiple Driving ranges (VRPMD)

| Vehicle Type | Vehicle capacity | Vehicle driving ranges (distance unit) | Symbol |
| :---: | :---: | :---: | :---: |
| ICEVs ${ }^{1}$ and/or PHEVs ${ }^{2}$ | Fixed to | No driving range limitation - Large | L |
| EVs | 100 | 200 - Medium | M |
| EVs |  | 100-Small | S |



## Capacitated Vehicle Routing Problem with Multiple Driving ranges (CVRPMD)



Develop an efficient solution method:

## Multi-Round Iterated Greedy

## Proposed solving method

## Multi-Round Iterated Greedy (MRIG)



## Analysis of the results

$\checkmark 33$ CVRP classical benchmark instances to solve both VRPMD and CVRPMD- are selected from a large number of instances
$\checkmark$ using different criteria to select these benchmark instances

- instances with an optimal or pseudo-optimal solution (instances from sets A, B, E, F, M and P)
- instances with information on routes for the optimal or pseudo-optimal solution
- mid-size instances including between 22 and 135 nodes.


## Distance-based cost evaluation

Measure the performance of the results by Relative Percentage Difference (RPD)

$$
\mathrm{RPD}=\frac{\text { Alg }_{s o l}-\text { Best }_{s o l}}{\text { Best }_{\text {sol }}} \times 100
$$

Best $t_{\text {sol }}$ : the best distance-based cost found through our results and the existing ones by Juan et al. (2014b), and the best known solutions (BKS) for any instance.
$A l g_{\text {sol }}$ : the distance-based cost obtained by the proposed algorithm

## Novel green indices for fleet configurations

$$
G I_{1}=\frac{S+\omega M}{S+M+L}
$$

$\omega \in[0,1]$.
The number of the used vehicle of types $\mathrm{S}, \mathrm{M}$ and L are denoted by S , $M$ and $L$, respectively.

The values of $\omega$ is set to 0.7 .

## Novel green indices for fleet configurations

$$
G I_{2}=\gamma S+\beta M+\alpha L
$$

This index measures environmental unit cost for each fleet configuration.

The values of $\alpha=100$

$$
\begin{aligned}
\beta & =30 \\
\text { and } \gamma & =10 .
\end{aligned}
$$

## Experimental results for VRPMD

Relation between Novel green indices


## Experimental results for VRPMD

| Instance name | Number of nodes | Capacity | BKS | MRHA |  | MRIG |  | $R P D$ |  | Diversified <br> Ratio |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Fleet $C F G$. $S / M / L$ | DBCost | Fleet $C F G$ $S / M / L$ | DBCost | M R H A | M RIG |  |
| A-n80-k10 | 80 | 100 | 1766.50 | 2/5/3 | 1776.19 | 2/5/3 | 1775.75 | 0.55 | 0.52 |  |
|  |  |  |  | 1/7/2 | 1785.05 | 1/7/2 | 1785.04 | 1.05 | 1.05 |  |
|  |  |  |  |  |  | 2/6/2 | 1794.42 | - | - | 2.5 |
|  |  |  |  |  |  | 0/9/1 | 1994.16 | - | - |  |
|  |  |  |  |  |  | 2/8/1 | 2016.21 | - | - |  |
| B-n57-k9 | 57 | 100 | 1603.63 | 0/4/5 | 1602.29 | 0/4/5 | 1602.29 | 0.00 | 0.00 | 1.6 |
|  |  |  |  | 0/5/4 | 1603.37 | 0/5/4 | 1603.37 | 0.07 | 0.07 |  |
|  |  |  |  | 0/6/3 | 1631.66 | 0/6/3 | 1631.85 | 1.83 | 1.84 |  |
|  |  |  |  | 1/3/5 | 1642.53 | 1/3/5 | 1636.34 | 2.51 | 2.13 |  |
|  |  |  |  | 1/4/4 | 1646.65 | 1/4/4 | 1637.44 | 2.77 | 2.19 |  |
|  |  |  |  |  |  | 1/5/3 | 1650.87 | - | - |  |
|  |  |  |  |  |  | 2/2/6 | 1694.09 | - | - |  |
|  |  |  |  |  |  | 0/7/2 | 1707.81 | - | - |  |
| E-n30-k3 | 30 | 4500 | 535.80 | 1/3/0 | 505.01 | 1/3/0 | 505.01 | 0.00 | 0.00 | 4 |
|  |  |  |  |  |  | 2/1/1 | 579.78 | - | - |  |
|  |  |  |  |  |  | 3/0/2 | 597.65 | - | - |  |
|  |  |  |  |  |  | $3 / 1 / 1$ | 633.37 | - | - |  |
| F-n135-k7 | 135 | 2210 | 1170.65 | 3/1/3 | 1175.73 | 3/1/3 | 1168.01 | 0.66 | 0.00 |  |
|  |  |  |  | $3 / 2 / 2$ | 1190.07 | $3 / 2 / 2$ | 1175.68 | 1.89 | 0.66 |  |
|  |  |  |  |  |  | 2/3/2 | 1171.18 | - | - | 2.5 |
|  |  |  |  |  |  | 1/5/1 | 1215.14 | - | - |  |
|  |  |  |  |  |  | 2/4/1 | 1241.70 | - | - |  |
| M-n121-k7 | 121 | 200 | 1045.16 | 2/3/2 | 1047.96 | 2/3/2 | 1044.64 | 0.32 | 0.00 | 2 |
|  |  |  |  | 1/7/0 | 1274.60 | 1/7/0 | 1287.52 | 22.01 | 23.25 |  |
|  |  |  |  |  |  | $3 / 2 / 3$ | 1050.66 | - | - |  |
|  |  |  |  |  |  | 1/5/1 | 1129.40 | - | - |  |
| P-n70-k10 | 70 | 135 | 830.02 | 8/2/0 | 834.38 | 8/2/0 | 843.63 | 0.53 | 1.64 | 2.5 |
|  |  |  |  | 10/0/0 | 841.56 | 10/0/0 | 851.39 | 1.39 | 2.57 |  |
|  |  |  |  |  |  | 6/4/0 | 841.42 | - | 1.37 |  |
|  |  |  |  |  |  | 9/1/0 | 844.35 | - | - |  |
|  |  |  |  |  |  | 7/3/0 | 842.36 | - | - |  |

Experimental results for 20 classical CVRP instances

## Experimental results for VRPMD

| Instance name | Number of nodes | Capacity | $B K S$ | $M R I G$ |  | RPD |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Fleet CFG. $S / M / L$ | Cost |  |
| A-n45-k7 | 45 | 100 | 1147.28 | 2/2/3 | 1146.77 | 0.00 |
|  |  |  |  | 1/4/2 | 1154.43 | 0.67 |
|  |  |  |  | 2/3/2 | 1155.60 | 0.77 |
|  |  |  |  | 1/5/1 | 1191.29 | 3.88 |
|  |  |  |  | 0/5/2 | 1174.01 | 2.38 |
|  |  |  |  | 0/6/1 | 1230.27 | 7.28 |
|  |  |  |  | 1/7/0 | 1463.93 | 27.66 |
|  |  |  |  | 2/4/1 | 1186.46 | 3.46 |
| E-n76-k7 | 76 | 220 | 687.60 | 3/4/0 | 690.20 | 0.38 |
|  |  |  |  | 4/3/0 | 695.26 | 1.11 |
|  |  |  |  | 5/2/0 | 705.97 | 2.67 |
|  |  |  |  | 6/1/0 | 733.74 | 6.71 |
| F-n45-k4 | 45 | 2010 | 724.57 | 1/2/1 | 723.54 | 0.00 |
|  |  |  |  | 2/0/2 | 792.37 | 9.51 |
| P-n101-k4 | 101 | 400 | 692.28 | 0/3/1 |  | 0.00 |
|  |  |  |  | 0/4/0 | 694.67 | 0.49 |
|  |  |  |  | 1/1/2 | 703.91 | 1.83 |
|  |  |  |  | 1/2/1 | 700.88 | 1.39 |
|  |  |  |  | 2/3/0 | 729.90 | 5.59 |

Experimental results for additional classical VRP instances

## Experimental results for VRPMD

$G I_{2} i=1 / G I_{2}$
Alternative Fleet Configurations for A-n45-k7
(distance-based Cost vs. Gl1 vs. GI2i)


## Experimental results for VRPMD

Gaps w.r.t. the BKS of the VRP without driving-range limitations


## Experimental results for CVRPMD

| Instance <br> name ( $Q_{0}$ ) | BKS Cost | VS-VM-VL | SetGI ${ }_{1}$ |  |  |  |  | $S e t G I_{2}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & \text { Fleet CFG. } \\ & \text { S/M/L } \end{aligned}$ | DBCost | $G I_{1}$ | $G I_{2}$ | $R P D$ | $\begin{aligned} & \text { Fleet CFG. } \\ & \text { S/M/L } \end{aligned}$ | DBCost | $G I_{1}$ | $G I_{2}$ | $R P D$ |
| P-n40-k5(140) | 461.73 | 112-140-175 | 0/1/3 | 431.67 | 0.18 | 330 | 0.00 |  |  |  |  |  |
|  |  |  | $0 / 0 / 4 L_{s}$ | 432.23 | 0.00 | 400 | 0.13 | 2/0/4 $L_{s}$ | 584.80 | 0.33 | 420 | 35.47 |
|  |  |  | $3 / 0 / 3{ }^{L} m$ | 457.78 | 0.50 | 330 | 6.05 | 4/0/2 ${ }^{L} m$ | 463.83 | 0.67 | 240 | 7.45 |
|  |  |  | $6 / 0 / 0^{L} l$ | 514.97 | 1.00 | 60 | 19.30 | $6 / 0 / 0^{L} l_{l}$ | 514.97 | 1.00 | 60 | 19.30 |
| P-n50-k10(100) | 699.56 | 80-100-125 | $0 / 0 / 8^{L_{s}}$ | 607.39 | 0.00 | 800 | 0.00 | $0 / 1 / 8 L_{s}$ | 658.36 | 0.08 | 830 | 8.39 |
|  |  |  | 5/0/5 ${ }^{L} m$ | 669.00 | 0.50 | 550 | 10.14 | $0 / 6 / 3^{L} m$ | 657.15 | 0.47 | 480 | 8.19 |
|  |  |  | 13/0/0 ${ }^{L}$ | 805.71 | 1.00 | 130 | 32.65 | 13/0/0 ${ }^{L}{ }_{l}$ | 805.71 | 1.00 | 130 | 32.65 |
| P-n55-k15(70) | 991.48 | 56-70-87 | $0 / 0 / 13^{L_{S}}$ | 824.21 | 0.00 | 1300 | 0.00 | $0 / 1 / 13^{L}{ }_{s}$ | 883.51 | 0.05 | 1330 | 7.20 |
|  |  |  | $8 / 0 / 8^{L} m$ | 915.58 | 0.50 | 880 | 11.09 | $3 / 8 / 4^{L} m$ | 919.94 | 0.57 | 670 | 11.62 |
|  |  |  | 20/0/0 ${ }^{L}$ | 1126.70 | 1.00 | 200 | 36.70 | 20/0/0 ${ }^{L}$ | 1126.70 | 1.00 | 200 | 36.70 |
| P-n65-k10(130) | 796.67 | 104-130-162 |  | 726.51 | 0.00 | 800 | 0.00 | $3 / 0 / 8^{L_{s}}$ | 831.83 | 0.27 | 830 | 14.50 |
|  |  |  | $5 / 0 / 5^{L} m$ | 779.95 | 0.50 | 550 | 7.36 | $0 / 6 / 3^{L} m$ | 766.30 | 0.47 | 480 | 5.48 |
|  |  |  | 13/0/0 ${ }^{L}{ }_{l}$ | 931.96 | 1.00 | 130 | 28.28 | $13 / 0 / 0^{L}{ }_{l}$ | 931.96 | 1.00 | 130 | 28.28 |
| P-n70-k10(135) | 830.02 | 108-135-196 | $0 / 0 / 8{ }^{L_{s}}$ | 760.93 | 0.00 | 800 | 0.00 | $1 / 1 / 8 L_{s}$ | 916.60 | 0.17 | 840 | 20.46 |
|  |  |  | 5/0/5 ${ }^{L} m$ | 821.68 | 0.50 | 550 | 7.98 | $1 / 6 / 3^{L} m$ | 812.82 | 0.52 | 490 | 6.82 |
|  |  |  | 13/0/0 ${ }^{L}$ | 969.13 | 1.00 | 130 | 27.36 | $13 / 0 / 0^{L} l$ | 969.13 | 1.00 | 130 | 27.36 |
| P-n76-k4(350) | 598.22 | 280-350-437 |  | 594.64 | 0.43 | 240 | 0.00 |  |  |  |  |  |
|  |  |  | $0 / 0 / 4^{L_{s}}$ | 695.78 | 0.00 | 400 | 17.01 | $2 / 1 / 4^{L_{S}}$ | 935.17 | 0.39 | 450 | 57.27 |
|  |  |  | 2/0/2 ${ }^{L} m$ | 606.86 | 0.50 | 220 | 2.06 | $0 / 2 / 2^{L} m$ | 597.13 | 0.35 | 260 | 0.42 |
|  |  |  | $8 / 0 / 0^{L} l_{l}$ | 744.71 | 1.00 | 80 | 25.24 | $8 / 0 / 0^{L}{ }_{l}$ | 744.71 | 1.00 | 80 | 25.24 |

Experimental results for CVRPMD with classical VRP instances

## Conclusion and future work

Extending the VRPMD:

- Multiple capacities for each type of vehicles
- developing an efficient method (MRIG)

D Developing reasonable solutions in terms of distance-based cost and more diverse solutions in terms of using greener fleet configurations.

Help decision makers to decide the best routes for their managerial problems

## Conclusion and future work

- Multi-objective optimization models
integrating classical assumptions such as time windows and multi-depot
Considering the impact of the carrying load of the vehicles on the resource consumption

Universitat Oberta de Catalunya

